

## Problem Set 2

due: May 1, 2018

### Exercise 1

3 points

Find an example of a complete undirected graph  $K_n$ ,  $n \geq 3$ , together with a cost function  $c : E(K_n) \rightarrow \mathbb{R}_{\geq 0}$  such that the optimal Traveling Salesman tour visiting each vertex at least once is not a Hamiltonian circuit.

### Exercise 2

4 points

Let  $G = (V, E)$  be an undirected graph with a cost function  $c : E \rightarrow \mathbb{R}_{\geq 0}$ . Reduce the following problem to TSP: Find a – not necessarily closed – walk of minimum cost w.r.t.  $c$  in  $G$  such that each vertex is visited at least once.

### Exercise 3

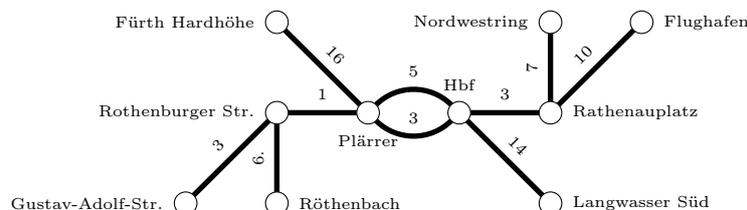
3 points

Let  $G = (V, E)$  be an undirected graph with a weight function  $w : E \rightarrow \mathbb{R}$ . Write the minimum-weight perfect matching problem on  $(G, w)$  as an integer program.

### Exercise 4

10 points

Let  $G$  be the following weighted undirected graph (U-Bahn Nürnberg, data is online):



(a) Compute the complete graph  $K_{10}$  and the length function  $\ell : E(K_{10}) \rightarrow \mathbb{R}_{\geq 0}$  satisfying

$$\ell(\{v, w\}) = (\text{weighted}) \text{ length of shortest path in } G \text{ from } v \text{ to } w$$

for all unordered pairs  $\{v, w\}$  of distinct vertices in  $G$ .

(b) Write a TSPLIB file and use `concorde` to solve the TSP on  $(K_{10}, \ell)$ .

- TSPLIB file format (use `EDGE_WEIGHT_FORMAT: FULL_MATRIX`, separate the entries by whitespaces, and the rows by line breaks):  
<http://plato.asu.edu/tsplib.pdf>
- `concorde`:  
<http://www.math.uwaterloo.ca/tsp/concorde/index.html> (download)  
<https://neos-server.org/neos/solvers/co:concorde/TSP.html> (online)

(c) Write down the shortest Traveling Salesman tour visiting each vertex in  $G$  at least once. What is its length?

If you solve (a) by programming, then send the code. Please submit also the TSPLIB file.