Wintersemester 11/12

Technische Universität Berlin Institut für Mathematik

# **Computational Integer Programming**

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## Exercise sheet 11

Deadline: Thu, 19 Jan. 2012, by email to koch@zib.de

### Exercise 1.

### 20 points

10 points

Model finding (semi) Magic Knight Tours on an  $n \times n$  board using ZIMPL. Solve the model with SCIP and report the largest n for which you can find a solution.

A description of Magic Squares can be found here: http://en.wikipedia.org/wiki/Magic\_square

A description of Knight Tours can be found here: http://en.wikipedia.org/wiki/Knight%27s\_tour

A (semi) Magic Knight Tour is a semi Magic Square, where the sequence of fields with increasing numbers forms a knights tour.

Details:

- We only want a semi Magic Spuare, i.e., the sums of the diagonals do not need to have a specific value.
- The numbers used for the fields of the Magic Square of size  $n \times n$  should be in range  $1 \dots n^2$ .
- The starting field is arbitrary, i.e., it is your choice. There are no restrictions.
- The Knights Tour can be a path, i.e., the last field need not to be anywhere related to the first field.

### Exercise 2.

Find the missing part in the proof for the quality of the Christophides TSP heuristics presented in the lecture.